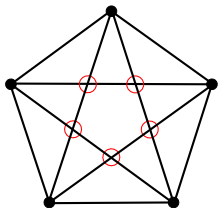
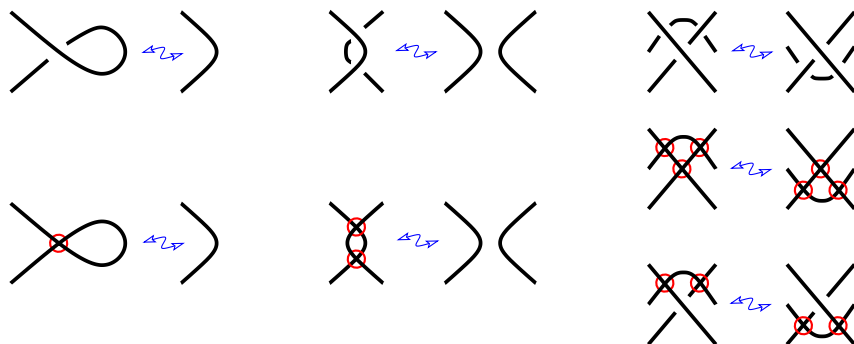


(Virtual) links [Ka2].

Virtual crossings

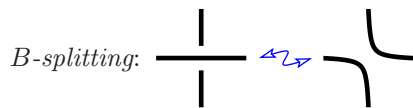
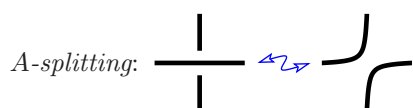


Reidemeister moves



The Kauffman bracket and the Jones polynomial [Ka1]

Let L be a link diagram.



A *state* S is a choice of either A - or B -splitting at every classical crossing.

$$\alpha(S) = \#(\text{of } A\text{-splittings in } S)$$

$$\beta(S) = \#(\text{of } B\text{-splittings in } S)$$

$$\delta(S) = \#(\text{of circles in } S)$$

$$[L](A, B, d) := \sum_S A^{\alpha(S)} B^{\beta(S)} d^{\delta(S)-1}$$

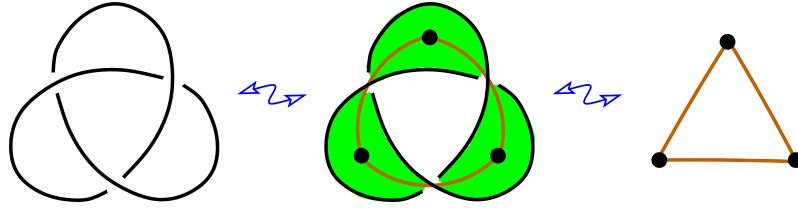
$$J_L(t) := (-1)^{w(L)} t^{3w(L)/4} [L](t^{-1/4}, t^{1/4}, -t^{1/2} - t^{-1/2})$$

Example

(α, β, δ)	$(3, 0, 1)$	$(2, 1, 2)$	$(2, 1, 2)$	$(1, 2, 1)$
$(2, 1, 2)$	$(1, 2, 1)$	$(1, 2, 3)$	$(0, 3, 2)$	

$$[L] = A^3 + 3A^2Bd + 2AB^2 + AB^2d^2 + B^3d; \quad J_L(t) = 1$$

Thistlethwaite's Theorem [Ka1] *Up to a sign and multiplication by a power of t the Jones polynomial $J_L(t)$ of an alternating link L is equal to the Tutte polynomial $T_\Gamma(-t, -t^{-1})$.*



REFERENCES

- [Ka1] L. H. Kauffman, *New invariants in knot theory*, Amer. Math. Monthly **95** (1988) 195–242.
- [Ka2] L. Kauffman, *Virtual knot theory*, European Journal of Combinatorics, **20** (1999) 663–690.