

Math 5102
due Mon **April 1**, 2019

Homework 5

1. Find the Green's function for the Bessel operators

a)
$$Lu = -\frac{d}{dx}x\frac{du}{dx}$$

b)
$$Lu = -\frac{d}{dx}x\frac{du}{dx} + \frac{n^2}{x}u$$

with the boundary conditions $u(0)$ finite and $u(1) = 0$.

2. a) Find the Green's function for the problem

$$L = -\frac{d^2}{dx^2} + \omega^2, \quad u(a) = 0, \quad u(b) = 0$$

for $a < b$ and ω a constant.

b) Does this Green's function exist for all values of ω ? If not, then what are the exceptional values for ω ?

3. Find (as an integral) the solution to the boundary value problem

$$u'' + 3u' = f, \quad u(0) = 1, \quad u'(1) = 6$$

4. Find the Green's function for the problem

$$u''' = f, \quad u(0) = 0, \quad u''(0) = 0, \quad u'(1) = 0$$