

Quiz 2

NOTE: Answers without proper justification will receive NO credit

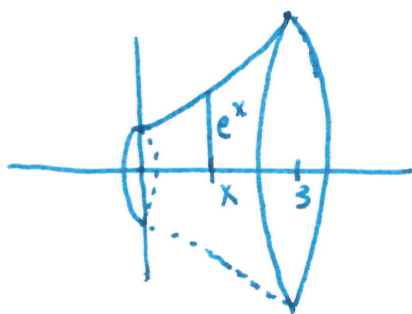
Problem 1. (2 points) Compute the integral $\int_0^2 x^2 \sqrt{x^3 + 1} dx$.

Use substitution $u = 1 + x^3 \rightsquigarrow du = 3x^2 dx$ so $x^2 dx = \frac{du}{3}$

$$\begin{cases} x=0 & \text{gives} & u=1 \\ x=2 & \text{"} & u=9 \end{cases}$$

$$\begin{aligned} \int_0^2 x^2 \sqrt{x^3 + 1} dx &= \int_1^9 \sqrt{u} \frac{du}{3} = \frac{1}{3} \frac{2}{3} u^{3/2} \Big|_1^9 = \frac{2}{9} (9^{3/2} - 1) = \frac{2}{9} (27 - 1) \\ &= \frac{2}{9} (27 - 1) = \boxed{\frac{52}{9}} \end{aligned}$$

Problem 2. (3 points) The area under the curve $y = e^x$ from $x = 0$ to $x = 3$ is revolved about the x -axis. Find the volume generated in this way.



$$\begin{aligned} A &= \int_0^3 \pi (e^x)^2 dx \\ &= \int_0^3 \pi e^{2x} dx \\ &= \int_0^6 \pi e^u \frac{du}{2} \end{aligned}$$

$$\begin{aligned} u &= 2x \\ du &= 2dx \end{aligned}$$

$$\begin{cases} x=0 & \text{gives} & u=0 \\ x=3 & \text{"} & u=6 \end{cases}$$

$$= \frac{\pi}{2} e^u \Big|_0^6 = \frac{\pi}{2} (e^6 - e^0) = \boxed{\frac{\pi}{2} (e^6 - 1)}$$