Math 2568 Section 30 - Linear Algebra

Autumn 2020

Instructor: Prof. Maria Angelica Cueto (cueto.5@osu.edu)

Contact information: All electronic communications for this course should be done via the messaging tools on Carmen. We kindly request you not to email the instructor directly.

Course information

Websites: https://carmen.osu.edu

https://people.math.osu.edu/cueto.5/teaching/2568/Au20

Lectures: M-W-F 9:10am-10:05am (in hybrid format).

Monday lectures will be held in-person at McPherson Chemical Lab (MC) 2015, while Wednesday and Friday lectures will be held online on Carmen Zoom.

On Monday's we will take the opportunity to answer questions, and giving an overview of the material that will be covered during the week. Further explanations will be provided in video format and lecture notes posted on Carmen. This will allow us to accommodate health issues (including positive diagnosis, symptoms, quarantine required following contact tracing; or potential suspension of in-person classes by university mandate).

Wednesday and Friday lecture will be delivered live over Zoom. You are expected to participate in them. Class material (lecture notes and slides), as well as a recording of the Zoom session (to accommodate special situations) will be posted on Carmen after class.

Office Hours: TBD (and by appointment), held online via Zoom. Questions can also be posted on Carmen's discussion boards.

Textbook: L.W. Johnson, R.D. Riess, J.T. Arnold: *Introduction to Linear Algebra*, 5th edition, Pearson.

Course description: This hybrid course is designed to introduce ideas from linear algebra, with emphasis on both its theoretical and practical aspects. Topics include matrix algebra, vector spaces and linear maps, bases and dimension, eigenvalues and eigenvectors, applications.

Prerequisites: A grade of C- or above in 1172, 1544, 2153, 2162.xx, 2182H, or 4182H; or a grade of C- or above in both 1152 and CSE 2321; or credit for 154, 254.xx, 263.xx, 263.01H, or 264H. Not open to students with credit for 4568 (568), 5520H (520H), or 572.

Course Content: The course will be divided into four parts (covering Chapters 1 through 6 of the textbook). In the first part, we will study matrices and linear systems of equations. In the second part, we will review vectors in the plane and in space, and extend this to higher dimensions. We will study the notion of a vector space in \mathbb{R}^n , subspaces, linear independence, dimension, bases of subspaces, orthonormal bases, and linear maps. In the third part, we will work with abstract vector spaces, and extend the constructions done for \mathbb{R}^n to the abstract setting. We will also discuss determinants of square matrices and their properties. In the last part of the course we will discuss the notion of eigenvalues and eigenvectors, both over real and complex numbers. A detailed list of

topics can be found below.

Coursework submissions: You will be submitting all coursework (homework and solutions to exams) exclusively through Carmen, and in pdf format. This document can be generated in two ways which will not cause major disruptions to what you have been doing for past courses. For those of you who have access to a tablet, this should be simple (e.g. by using Notability on an Ipad). Otherwise, you can scan your handwritten solutions with your smartphone and generate a pdf. There are several apps and tutorials online for this, see, e.g.

https://edu.gcfglobal.org/en/mobile-device-tips/how-to-scan-documents-with-a-smartphone/1/.

Grading. The grade will be based on homework assignments (20%), three midterms (20% each), and the final exam (20%). Your course letter grade will then be determined based on: (1) your course percentile (your relative rank among your peers), and (2) my determination of the overall class performance level.

A reasonable percentile-to-letter-grade **estimate** is the following:

Letter grade	A	A-	B+	В	B-	C+	С	C-	D	E
Percentile range	100-90	90-85	85-80	80-70	70-65	65-60	60-40	40-35	35-20	20-0

If your degree program requires a certain letter grade in this course, it is a good idea to think about the likelihood of you ending up in each of the above ranges above early in this semester.

Homework: Homework is an essential component of this course. Problems will be assigned from the course's textbook. The goal of each homework set is to help you understand the material and to prepare you for the tests. It is thus imperative that you start working on each assignment as soon as we view the material in class. Take time to understand the questions and think about how to solve each problem before seeking help from the instructors and your classmates. Feel free to post questions on Carmen discussion board if you are stuck on a problem.

You are strongly encouraged to discuss the problems with me and your classmates, but your write ups must be your own. If you use other people's ideas, including from an online source, you must state this explicitly. Active participation on Carmen discussion forum will contribute towards your homework grade.

There will be a total of 11 homeworks this semester (see the course schedule for due dates). Each homework will be graded for correctness and clarity of explanations. Only three problems from each set will be graded. Each homework set will be worth 20 points (5 points per problem graded plus 5 extra points for completion). No late homework will be accepted without medical excuse, but the lowest score will be dropped.

Exams: There will be four exams: three midterms and one final exam. Exams will take place online through Carmen, outside regular class hours (see dates below). Special office hours will be held on midterm dates during normal class time in lieu of regular lectures.

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Midterm 1: Monday Sept. 21, 2020 (4:00-6:00pm). Topics: \S1.1 - 1.3, 1.5 - 1.7, 1.9.
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Midterm 2: Monday, Oct. 19, 2020 (4:00-6:00pm). Topics: $\S 2.1 - 2.4, 3.1 - 3.7$.

Midterm 3: Monday, Nov. 16, 2020 (4:00-6:00pm). Topics: $\S5.1 - 5.4, 5.7 - 5.9, 6.1 - 6.4$.

Final: Tuesday, Dec. 8, 2020 (10:00-11:45am). Topics: cumulative, focused on $\S4.1-4.7$.

All exams will be closed-book. All students are expected to abide by the rules of Academic integrity. Honesty is the foundation of good academic work. When you are solving the exams, avoid engaging in plagiarism, unauthorized collaboration, cheating, or facilitating academic dishonesty. For more information, see the *General policies* section below.

Mathematics is not just about deriving the correct numerical solution to a problem. It is also about convincing others that your method of calculation is appropriate. Insufficiently supported answers may receive partial or no credit on exams.

Class Participation and Attendance. Mathematics is a human activity. We will cover the material in an **interactive fashion** each lecture. Although this course will be conducted in a hybrid way (mostly, remotely), it is important to stay actively engaged with the material and connected with both the instructor and your classmates, e.g. by using Carmen's discussion board.

Online lectures will be approached as active learning sessions, in particular, through discussions in small groups. Lectures will be recorded to accommodate special situations, but I expect students to attend the lectures while they are being delivered. Frequent absences are likely to be noted and may factor into the grade in borderline cases.

Course Topics

The following is a complete list of each section of the textbook that we will cover this semester:

Ch. 1 Matrices and Systems of Linear Equations Ch. 4 The Eigenvalue Problem

- 1.1 Introduction to Matrices And Systems of Linear Equations
- 1.2 Echelon Form and Gauss-Jordan Elimina-
- 1.3 Consistent Systems of Linear Equations
- 1.5 Matrix Operations
- 1.6 Algebraic Properties of Matrix Operations
- 1.7 Linear Independence and Nonsingular Ma-
- 1.9 Matrix Inverses and Their Properties

Ch. 2 Vectors in 2-Space and 3-Space

- 2.1 Vectors in the Plane
- 2.2 Vectors in Space
- 2.3 The Dot Product and the Cross Product
- 2.4 Lines And Planes in Space

Ch. 3 The Vector Space \mathbb{R}^n

- 3.1 Introduction to the Vector Space \mathbb{R}^n
- 3.2 Vector Space Properties of \mathbb{R}^n
- 3.3 Examples of Subspaces
- 3.4 Bases for Subspaces
- 3.5 Dimension
- 3.6 Orthogonal Bases for Subspaces
- 3.7 Linear Transformation from \mathbb{R}^n to \mathbb{R}^m

- 4.1 The Eigenvalue Problem for 2×2 Matrices
- 4.2 Determinants and the Eigenvalue Problem
- 4.4 Eigenvalues and the Characteristic Polyno-
- 4.5 Eigenvectors and Eigenspaces
- 4.6 Complex Eigenvalues and Eigenvectors
- 4.7 Similarity Transformations and Diagonalization

Ch. 5 Vector Spaces and Linear Transformations

- 5.1 Introduction to Vector Spaces and Linear Transformations
- 5.2 Vector Spaces
- 5.3 Subspaces
- 5.4 Linear Independence, Bases and Coordinates
- 5.7 Linear Transformations
- 5.8 Operations With Linear Transformations
- 5.9 Matrix Representations Of Linear Transformations

Ch. 6 Determinants

- 6.1 Introduction to Determinants
- 6.2 Cofactor Expansions Of Determinants
- 6.3 Elementary Operations And Determinants
- 6.4 Cramer's Rule

Course Technology

The course will be delivered in a hybrid format. For Wednesday and Friday lectures, as well as office hours, you should be able to connect to CarmenZoom with audio, video and chat participation. Course annoncements will be made through Carmen. It is strongly encouraged that you connect to Carmen regularly (at least three times a week).

If you are concerned about privacy, you are welcome to use the virtual background feature provided by Zoom. For help setting up your personal background see:

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https://support.zoom.us/hc/en-us/articles/210707503-Virtual-Background
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For help with your password, university e-mail, Carmen, or any other technology issues, questions, or requests, contact the OSU IT Service Desk. Standard support hours are available at

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https://ocio.osu.edu/help/hours.
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Support for urgent issues is available 24x7.

- Self-Service and Chat support: http://ocio.osu.edu/selfservice
- Email: 8help@osu.edu; Phone: 614-688-HELP (4357); TDD: 614-688-8743.

HEALTH AND SAFETY POLICIES

All students, faculty and staff are required to comply with and stay up to date on all university safety and health guidance (see https://safeandhealthy.osu.edu), which includes following university mask policies and maintaining a safe physical distance at all times. Non-compliance will be warned first and disciplinary actions will be taken for repeated offenses.

To attend events on campus (such as in-person classes), you must complete daily health checks and get approval to be on campus *before you come to class*. This daily check will be reported through the Ohio State mobile app or https://compass.osu.edu. You must self-isolate if running a fever or in other ways symptomatic.

Face masks must be worn in indoor settings, including, but not limited to: classrooms, residence halls, conference rooms, shared office spaces, hallways, buses, shared vehicles and common areas such as lobbies, study spaces and laundry facilities on all Ohio State campuses. Masks must also be worn in outdoor spaces on campus, even when individuals can maintain appropriate physical distancing.

Masks must be worn at all times during in-person classes. Social distancing will be required as well. You will not be allowed in class without following these rules. To facilitate contact-tracing, at the beginning of each in-person session, each student will record their seating assignment and submit this information through Carmen (a chart of the classroom will be provided).

Additional resources

The Ohio State University Wexner Medical Center's Cornavirus Outbreak site includes the latest information about COVID-19 as well as guidance for students, faculty and staff.

The Keep Learning site includes tips and resources to help students make the shift to hybrid and online learning, addressing strategies for success as well as technology tools.

The Office of Student Life's "We Are Here For You" page includes several resources to support your mental, physical and financial health.

GENERAL POLICIES

Academic Misconduct Statement: It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term academic misconduct includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-48.7). For additional information, see the Code of Student Conduct at http://studentlife.osu.edu/csc/.

Statement on Title IX: Title IX makes it clear that violence and harassment based on sex and gender are Civil Rights offenses subject to the same kinds of accountability and the same kinds of support applied to offenses against other protected categories (e.g., race). If you or someone you know has been sexually harassed or assaulted, you may find the appropriate resources at http://titleix.osu.edu or by contacting the Ohio State Title IX Coordinator, Kellie Brennan, at titleix@osu.edu

Disability Statement: The university strives to make all learning experiences as accessible as possible. In light of the current pandemic, students seeking to request COVID-related accommodations may do so through the university's request process, managed by Student Life Disability Services. If you anticipate or experience academic barriers based on your disability (including mental health, chronic, or temporary medical conditions), please let me know immediately so that we can privately discuss options. To establish reasonable accommodations, I may request that you register with Student Life Disability Services. After registration, make arrangements with me as soon as possible to discuss your accommodations so that they may be implemented in a timely fashion. SLDS contact information: slds@osu.edu; 614-292-3307; http://www.ods.osu.edu/; 098 Baker Hall, 113 W. 12th Avenue.

Your mental health: As a student you may experience a range of issues that can cause barriers to learning such as strained relationships, increased anxiety, alcohol/drug problems, feeling down, difficulty concentrating and/or lack of motivation. These mental health concerns or stressful events may lead to diminished academic performance or reduce a students ability to participate in daily activities. The Ohio State University offers services to assist you with addressing these and other concerns you may be experiencing. If you or someone you know are suffering from any of the aforementioned conditions, you can learn more about the broad range of confidential mental health services available on campus via the Office of Student Lifes Counseling and Consultation Service (CCS) by visiting https://ccs.osu.edu or calling 614- 292-5766. CCS is located on the 4th Floor of the Younkin Success Center and 10th Floor of Lincoln Tower. You can reach an on-call counselor when CCS is closed at 614-292-5766. Emergency help is also available through the 24/7 National Suicide Prevention Hotline at 1-800-273- TALK or at https://suicidepreventionlifeline.org

Course Schedule

A detailed day-by-day tentative schedule for this course is available below. This includes topics to be covered on each lecture, homework due dates and exam. You will be notified of any changes by Carmen announcements. The most recent version of this syllabus will remain available at the course's webpage.

Monday	TUESDAY	Wednesday	Thursday	FRIDAY
Aug 24th	25th	26th	27th	28th
		§1.1 (I)		§1.1 (II), 1.2 (I)
31st	Sep 1st	2nd	3rd	4th
§1.2 (II)		§1.3 (I) HW01		§1.3 (II)
7th	8th	9th	10th	11th
No class		§1.5		$\S1.6,1.9(I)$ HW02
14th	15th	16th	17th	18th
§1.9(II)		§1.7		§2.1-2.2 HW03 Last day to drop without a "W"
21st	22nd	23rd	24th	25th
Midterm 1 4:00-6:00pm		§2.3 (I)		§2.3(II),2.4(I)
28th	29th	30th	Oct 1st	2nd
§2.4 (II)		§3.1-3.2		§3.3
		HW04		
5th	6th	7th	8th	9th
§3.4		§3.5		§3.6 HW05
12th	13th	14th	15th	16th
§3.7 (I)		§3.7(II)		§5.1-5.2 HW06
19th	20th	21st	22nd	23rd
Midterm 2		§5.3		§5.4
4:00-6:00pm 26th	27th	28th	29th	30th
	27011		29011	§5.8
§5.7 (I)		§5.7 (II) HW07		Last day to drop w/o petitioning
Nov 2nd	3rd	4th	5th	6th
§5.9		§6.1-6.2 HW08		§6.3
9th	10th	11th	12th	13th
§6.4		No class		§4.1-4.2 HW09
16th	17th	18th	19th	20th
Midterm 3		§4.4		§4.5 (I)
4:00-6:00pm				

Monday	Tuesday	Wednesday	Thursday	FRIDAY	
23rd	24th	25th	26th	27th	
§4.5 (II), 4.6 (I)		§4.6 (II) HW10		No class	
30th	Dec 1st	2nd	3rd	4th	
§4.7 (I)		§4.7 (II)		Review HW11	
$7 ext{th}$	8th	9th	10th	11th	
	Final				
	10:00–11:45am				