## CORRECTION TO "THE COHOMOLOGY OF A COXETER GROUP WITH GROUP RING COEFFICIENTS"

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In Remark 5.8 on pages 309-310 of [1], I wrote, "It follows easily from Theorem A that if L(W, S) is a Cohen-Macaulay complex of dimension (n - 1), then W is a virtual duality group of dimension n." In fact, as I explain below, a further hypothesis is required.

Suppose that L is an *m*-dimensional simplicial complex, that T is (the vertex set of) a simplex in L, and that |T| denotes the number of vertices in T. A neighborhood of the barycenter of T in L is homeomorphic to the cone on  $S^{|T|-1}Lk(T,L)$ , the (|T|-1)-fold suspension of the link of T. Let  $c_T: L \to S^{|T|}Lk(T,L)$  be the map that is the identity on this neighborhood and collapses its complement to a point. Consider the following condition:

(d) for each simplex T in L,  $c_T^*: H^*(S^{|T|}Lk(T,L)) \to H^*(L)$  is injective.

Not every Cohen-Macaulay complex L satisfies condition (d). For example, if L is a triangulation of an *m*-disk, then condition (d) fails when T is a vertex in its interior.

The correct statement for Remark 5.8 is that if L(=L(W,S)) is an (n-1)dimensional Cohen-Macaulay complex for which condition (d) holds, then W is a virtual duality group of dimension n. To see this, first note that  $H^*(K^S) \cong$  $H^*(L)$  and that, by excision,  $H^*(K^S, K^{S-T}) \cong \overline{H}^*(S^{|T|}Lk(T,L))$  for any simplex T in L (i.e., for any  $T \in \mathscr{G}_{\geq \emptyset}^f$ ). So, condition (d) is equivalent to the condition where  $H^*(K^S, K^{S-T}) \to \overline{H}^*(K^S)$  is injective. Thus, if L is Cohen-Macaulay and condition (d) holds, then  $\overline{H}^*(K^{S-T})$  is concentrated in dimension (n-1) for any  $T \in \mathscr{G}^f$ . It then follows from Theorem A that  $H_c^*(\Sigma)$  is concentrated in dimension n, and hence, W is a virtual duality group.

## References

 M. W. DAVIS, The cohomology of a Coxeter group with group ring coefficients, Duke Math. J. 91 (1998), 297-314.

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