

# MATH 7721, SPRING 2018

Homework #23, March 2

## PROBLEMS

1. Show that  $\delta(J\nabla f) = 0$  for any smooth function  $f$  on a Kähler manifold.
2. As a (very narrow) special case of the Hodge decomposition theorem, every smooth differential 1-form has an exact-coclosed decomposition, in the sense of being the sum of an exact 1-form and one with zero divergence. Assuming compactness of  $M$  in addition to the other hypotheses required for equality (23.7) in the day-by-day list of topics, interpret (23.7), with any  $v \in \mathfrak{h}(M)$ , as an exact-coclosed decomposition of the 1-form  $-2\lambda g(v, \cdot)$ .
3. Verify the second parts of formulae (23.2) and (23.8) in the day-by-day list of topics.