

## Presentations

Wed, 2/3: 1.2 + 1.6 - William  
1.7 - Destiny

Fri, 2/5: 1.9 + 1.10 - Michael  
1.11 - Ashe

Mon, 2/8: 1.12 - Andie  
1.14 - Nathan

Wed, 2/10: 1.17 - Jacob  
1.20 - Morgan

## Daily Homework

Posted on website

Submit either on Canvas or by email

↳ must be in .pdf

CamScanner, Scannable, etc.

↳ Due by beginning of class (11 AM)

Recall: If  $d$  and  $n$  are integers, then we say  $d$  divides  $n$ , written  $d|n$ , if there is an integer  $k$  such that  $n = d \cdot k$ .

Def: If  $a$ ,  $b$ , and  $n$  are integers, and  $n > 0$ , then we say  $a$  and  $b$  are congruent modulo  $n$  if  $n|(a-b)$ . We denote this by writing

$$a \equiv b \pmod{n}.$$

Ex:  $6 \equiv 9 \pmod{3}$  because  $3|(6-9) \rightarrow 6-9 = -3 = 3 \cdot (-1)$

Ex: If  $a$  and  $b$  are any integers, then  $1|(a-b)$ , because  $a-b = 1 \cdot (a-b)$  so  $a \equiv b \pmod{1}$ .

Ex: The case where  $n = 2$ .

Then  $a \equiv b \pmod{2}$  means  $2 \mid (a - b)$

i.e.  $(a - b) = 2 \cdot k$  for an integer  $k$ .

$$\rightarrow a = b + 2k$$

$\Rightarrow$  if  $b$  is even, then so is  $a$

$$\rightarrow b = a - 2k$$

$\Rightarrow$  if  $a$  is even, then so is  $b$

Similarly, if one is odd, then so must be the other.

Conclude:  $a \equiv b \pmod{2}$  means either

$a$  and  $b$  are both even

or

$a$  and  $b$  are both odd.