HW: nent/legible

name at top!

staple or paperclip if necessary

complete sentences

andience is your classmates

collaborate responsibly

Last time: - and A

Warm-Up: Chech that

· PAQ = QAP

· PA(QAR) = (PAQ)AR

That is, A is commutative and associative.

PAQ is true exactly when at least one of Por Q is true.

P	Q	PVQ
T	T	T
T	F	T
F	T	T
F	F	F

Note:
$$P \vee Q = Q \vee P$$

 $P \vee (Q \vee R) = (P \vee Q) \vee R$

How do the operations -, 1, V interact with one another?

Then
PAQ is "mis even and nis odd."

This becomes false if m is not even OR n is not odd.

i.e. - (PAQ) is true

= -PV-Q

In general, ne have:

Thm (De Morgan's Laws) Let P and Q be sentences. Then

(a) - (PAQ) is logically equivalent to -PV-Q (b) ¬ (PVQ) is logically equivalent to ¬P 1 ¬Q

Proof of (a):

By truth table:

<u>P</u>	Q	PAQ	- (PAQ)	¬P	¬Q	-PV-Q
T	T	T	F	F	F	F
T	F	F	T	II	T	T
F	T	F	T	7	F	T
F	F	F	〒	T	T	T

We can also prove this by giving an explanation in words:

We nish to show ¬(PAQ) always has the same truth value as ¬PV¬Q.

First, suppose ¬(PAQ) is true. Then PAQ is false, so at least one of P or Q is false.

But this means at least one of ¬P or ¬Q
is true, so ¬P V ¬Q is true.

In words:

Next, suppose - (PAQ) is false. Then
PAQ is true, so both P and Q are true.

Now, both -P and -Q will be false, menning -PV-Q is false as well.

(P) HM 1