$\mathbf{1}$ List all subgroups of $\mathbb{Z}_{45}$, giving a generator for each. Draw the subgroup lattice.

2 (Judson 4.24 - modified) Let $p$ and $q$ be distinct prime numbers.
(a) How many generators does $\mathbb{Z}_{p q}$ have?
(b) How many generators does $\mathbb{Z}_{p^{2}}$ have?

