

1. You roll a die 4 times. a) Find  $N$  (the number of outcomes in the sample space).  
b) If  $E$  is the event: "All 4 rolls give the same number" find  $Pr(E)$ .

2. There are 5 men and 3 women in line to board a bus. a) In how many ways can they line up?  
b) What is the probability that the first two people in line are men?

3. a) Randomly choose 5 cards from a standard deck. What is the probability that you have no pairs (and therefore no three-of-a-kind or no four-of-a-kind either)?

- b) You flip a coin 12 times. What is the probability that you will get exactly 6 heads?

Evaluate the following: And give an example of what they would count

$${}_{80}C_2$$

$${}_{80}P_3$$

$${}_{80}C_{78}$$

$${}_{10}P_4$$

Find the probability of getting a total of 4 when rolling two fair dice.

Find the probability of getting at least 9 when you roll two fair dice.

### 5. State the Rule, Criterion or Paradox described below:

a) Randy wins an election. A new election is held and the only difference is that some people that had initially voted for Sandy now vote for Randy. Randy should win the new election.

b) Randy has 185 pieces of candy to divide among his 12 children. He prepares to divide them according to how many chores each child has done. His son Andy will receive 19 pieces of candy. Just before handing out the candies Randy finds another candy and redistributes them. Now Andy gets just 18 pieces.

c) Sandy wins an election. After the election it is determined that another candidate, Mandy, was not a legitimate candidate so her name is removed from the preference schedule and the votes are recounted. Sandy should win the new election.

d) There are 3 nursing shifts and 79 nurses to staff these shifts (exactly one shift per nurse). The standard quota for the first shift is 32.8. The first shift should be staffed by either 32 or 33 nurses.

e) Randy has 185 pieces of candy to divide among his 12 children. He prepares to divide them according to how many chores each child has done. His son Andy will receive 9 pieces of candy and his daughter Mandy will receive 28 pieces. Just before handing out the candies the father Randy determines that Mandy and some other children (but not Andy) have done some additional chores. Randy redistributes the candies and now Andy gets 10 and Mandy gets 27 pieces.

Number of Voters	21	11	15	13
First Choice	B	A	A	D
Second Choice	D	D	D	C
Third Choice	C	B	C	B
Fourth Choice	A	C	B	A

6. For the preference schedule above, determine the ranking according to the extended Plurality with elimination method.

7. For the preference schedule above, determine the ranking according to the recursive Plurality method

Number of Voters	21	11	15	13
First Choice	B	A	A	D
Second Choice	D	D	D	C
Third Choice	C	B	C	B
Fourth Choice	A	C	B	A

For the preference schedule shown above, determine the winner by the method of pairwise comparisons.

For the preference schedule shown above, determine the winner by the method of the Borda count.

9. Given the populations for the states A,B,C,D and E below determine the apportionment of 87 seats using Adams' method. Hint: One of the following will work as a modified divisor for this situation: 23.5, 24.1, 24.7, 25.3, 25.9. Write down your successful modified divisor and the apportionments. a) Successful Modified Divisor:                      b) Apportionments:    A =        B =        C =        D =        E =

States	Pop.									
A	499									
B	197									
C	457									
D	756									
E	127									

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10. Do the apportionment for problem 9 using Hamilton's Method and 87 seats.

**Alabama paradox** occurs *when an increase in the total number of seats being apportioned, in and of itself, forces a state to lose one of its seats*

**population paradox**- when state A loses a seat to state B even though the population of A *grew at a higher rate* than the population of B.

**the new-states paradox**- that *the addition of a new state with its fair share of seats can, in and of itself, affect the apportionments of other states.*

### **The Quota Rule**

No state should be apportioned a number of seats smaller than its lower quota or larger than its upper quota.

### **The Majority Criterion**

If candidate X has a *majority* of the 1<sup>st</sup> place votes, then candidate X should be the *winner* of the election.

### **The Condorcet Criterion**

If candidate X is preferred by the voters over each of the other candidates in a head-to-head comparison, then candidate X should be the winner of the election.

### **The Monotonicity Criterion**

If candidate  $X$  is a winner of an election and, in a reelection, the only changes in the ballots are changes that favor  $X$  (and only  $X$ ), then  $X$  should remain a winner of the election.

### **The Independence-of-Irrelevant-Alternatives Criterion (IIA)**

If candidate  $X$  is a winner of an election and in a recount one of the non-winning candidates is removed from the ballots, then  $X$  should still be a winner of the election.