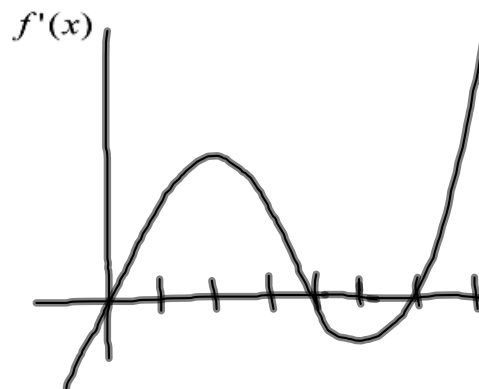


Math 152 Calculus and Analytic Geometry II

Sec 4.9 Antiderivatives

Suppose you are given the derivative of a function, $f'(x)$.
Can you find the original function?

$$f'(x) = 4x^3 + 10x - 7$$



Definition: A function F is called the antiderivative of f on an interval I if

$$F'(x) = f(x) \quad \text{for all } x \text{ in the interval } I.$$

Much of our time in 152 will be spent learning how to find antiderivatives and what applications they have.

Can a function have more than one antiderivative?

Theorem: If F is an antiderivative of f on an interval I , then all antiderivatives of f are of the form

$$F(x) + C$$

$$x^n$$

Table of common antiderivatives

$$cf(x)$$

$$\frac{1}{x}$$

$$f(x) + g(x)$$

$$e^x$$

$$x$$

$$\frac{1}{1+x^2}$$

$$x^2$$

$$x^3$$

$$\frac{1}{\sqrt{1-x^2}}$$

$$\cos(x)$$

$$\sin(x)$$

$$\sec^2(x)$$

$$\sec(x) \tan(x)$$

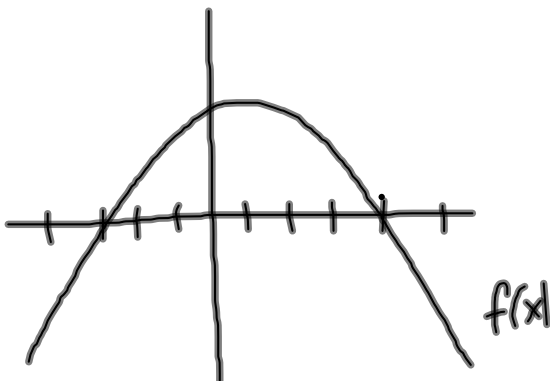
Differential Equations

Find $f(x)$ where $f'(x) = 3x^2 - 6x - 9$ $f(1) = -5$

Find the antiderivative that satisfies the condition.
Also graph the derivative, and use that to graph the function.

Geometry of Antiderivatives.

Draw the antiderivative of $f(x)$ given that $F(0)=2$.



Another way to do it if you are given an equation for the derivative $f(x)$
Use "Direction Fields"

Double click on $f(x)$ on the left to change the derivative (slope) function.

<http://www.math.ohio-state.edu/>

[~maharry/GeoGebra/SlopeFieldGenerator02FromDaveMatthews.html](http://www.math.ohio-state.edu/~maharry/GeoGebra/SlopeFieldGenerator02FromDaveMatthews.html)



Rectilinear Motion: A ball is thrown upwards with a speed of 48 ft/sec from a cliff 400 feet high. Find its height after t seconds.

Start with $a(t) = 32$ (ft/sec)/sec.

Practice exercises:

Find the most general antiderivative:

$$f(x) = 1 - x^3 + 3x^5 - x^7$$

$$f(u) = \frac{u^3 - \sqrt{u}}{u^2}$$

$$f(x) = 4(5x^2 - 3x + 2)^3(10x - 3)$$

Problems to work on from Homework:

Find f .

$$f'(x) = 1 - 6x \quad f(0) = 8$$