

Math 152 Calculus and Analytic Geometry II

Sec. 7.2 Trigonometric Integrals

This section has suggestions for how to solve integrals involving certain combinations of trig functions.

For example.

$$\int \cos^3(x) dx$$

For Example:

$$\int \cos^3(x) \sin^5(x) dx$$

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$$\int \cos^3(x) \sin^5(x) dx$$

What about this?

$$\int \sin^2(x) dx$$

General Strategy:

$$\int \sin^{(\text{odd})}(x) \cos^{(\text{anything})}(x) dx$$

$$\int \sin^{(\text{anything})}(x) \cos^{(\text{odd})}(x) dx$$

What about

$$\int \tan^6(x) \sec^4(x) dx$$

Another one...

$$\int \tan^7(x) \sec^4(x) dx$$

General Strategy:

$$\int \tan^{(\text{anything})}(x) \sec^{(\text{even})}(x) dx$$

$$\int \tan^{(\text{odd})}(x) \sec^{(\text{anything})}(x) dx$$

Otherwise, harder, maybe try some identities...

$$\int \tan(x) dx = \ln|\sec(x)| \qquad \int \sec(x) dx = \ln|\sec(x) + \tan(x)|$$

HW Problems:

15. $\int \sin^3(x) \sqrt{\cos(x)} dx$

31. $\int \frac{\tan^5(x)}{\cos^4(x)} dx$

59. Rotate the given region about the x-axis

$$y = \sin(x)$$

$$x = \frac{\pi}{2}$$

$$x = \pi$$

$$y = 0$$